

## Subject Code—4274

## M.C.A. (Second Year) EXAMINATION

June, 2006

(5 Years Integrated Course))

(Re-appear)

## MATHEMATICS—II

MCA-205

Discrete Mathematical Structures

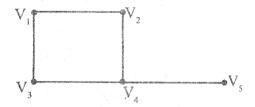
Time: 3 Hours Maximum Marks: 100

Note: Attempt any Five questions. All questions carry equal marks.

- (b) Define a Subgroup. Let H be a subgroup of G, then prove that the right cosets Ha form a partition of G.
- (c) Explain the following:
  - (i) Normal subgroup
  - (ii) Semi-group and Free semi-group.
- (a) Define a grammar and language of a grammar. Discuss also various types of grammars.
  - (b) Define a finite-state machine. Design a finite-state machine that performs serial addition.
  - (c) Describe the following:
    - (i) Finite graph
    - (ii) Length of path
    - (iii) Cut points and bridges
    - (iv) Subgraphs.
- 3. (a) If a simple graph G with n vertices has more than  $\frac{1}{2}(n-1)(n-2)$  edges, then prove that G is connected.

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(b) Use adjacency matrix to represent the graph shown in figure :



4. (a) Draw the graph represented by the incidence matrix:

- (b) Describe an efficient algorithm for comparing distances in graphs.
- (c) Describe Infix, Prefix and Postfix form of an algebraic expression in trees.
- 5. (a) Define partially ordered sets. Consider P(s) as the power set, show that the inclusion relation ⊆ is a partial ordering on the powerset P(s).

- (b) Explain bounded lattice and Hasse diagram. Draw the Hasse digram of (P(A), ⊆), where:
  - (i)  $A = \{0, 1\}$
  - (ii)  $A = \{0, 1, 2, 3\}$
- 6. (a) What do you mean by Boolean Algebra?

  Prove the following for Boolean Algebra:
  - (i) The zero and unit elements are unique
  - (ii) The complement of an element is unique.
  - (b) Prove that:
    - (i)  $a + (\overline{a}.b) = a + b$  and

$$a.(\overline{a}+b)=a.b$$

(ii) 
$$(a+b).(\overline{b}+c)+b.(\overline{a}+\overline{c}) = a.\overline{b}+a.c+b$$

- 7. (a) Show that  $(p \land q) \rightarrow (p \lor q)$  is a tautology.
  - (b) With the help of truth tables, prove that:

$$p \lor \sim q = (p \lor q) \land \sim (p \land q)$$

(c) Write a short note on gate circuits.

- 8. (a) Explain an integral domain and a finite field.
  - (b) Show that the set S of all matrices of the form  $\begin{pmatrix} a & b \\ -b & a \end{pmatrix}$ , where  $a, b \in \mathbb{R}$  is a field with respect to matrix addition and matrix multiplication.
  - (c) Let  $f(t) = t^4 3t^3 + 3t^2 + 3t 20$ . Find all the roots of f(t) given that t = (1+2i) is a root.